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Electro- Hydrodynamic Peristaltic Transport of a Third-Grade Nanofluid Flow in the Presence of Thermal Radiation in an Asymmetric Channel

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ABSTRACT

This work finds application in micro-fabrication techniques and the chemical industry. This study examines the effects of the magnetic field and electroosmotic repulsion on the peristaltic flow of a third-grade nanofluid in an asymmetric channel. The problem is modelled with the aid of a lubrication approach. The expressions for stream function, velocity, temperature, and species concentration are derived using the Adomian decomposition method. The physical parameters are analyzed and discussed graphically. The significant outcome of this work is to analyze the flow behaviour in both symmetric and asymmetric channels. The results are used to analyze the blood flow through channels, which helps examine the artery blockage treatment and cancer tumour elimination. The velocity profile with the impact of Deborah's number and the electroosmotic parameter is studied for both channels. Validation of obtained results is done in comparison with the previous results.

Keywords: Peristaltic flow, Electroosmosis, Adomian Decomposition Method (ADM), Thermal radiation.

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1. INTRODUCTION

The study of electro-osmosis has received a lot of attention over the past few decades. It is possible to modify peristaltic motion by increasing and decreasing external electric fields. One such example is the incorporation of peristaltic flow using electro-osmosis [1]. Electro-osmotic transport is a prominent topic in microfluidics because of its present applications in healthcare investigations, scientific and biological analysis, cardiac output issues, medicine, and treating ailments like abnormal and sickle cell disease. The investigation of fluid flow is influenced by an external electric field known as electro-osmosis. A charge is generated when an electrolyte solution arrives in contact with the solid interface. When ions are drawn in opposite directions by the surface's electric potential, it leads to the creation of an electron dual layer (EDL). Inducing fluid mobility in an ionic solution with an electric field involves applying an electric charge's net kinetic coupling force. In order to control fluid flow through channels, this phenomenon is used in bio-microfluidics. Electro-osmotic pumps swiftly and easily produce high-pressure liquid flow while being affordable, effective, and lightweight. It is essential to create precise models of electro-osmotic transport using the elastic constants for non-Newtonian and Newtonian fluids and electro-osmotic transit systems in order to comprehend physiological systems and create useful bio-devices. There have been some recent studies on electro-osmotic transfers [2–5].

Due to its usage in engineering, biomedicine, and industry, the magnetic field has attracted much attention. Strong magnetic fields are essential for the operation of electric power generators, electrostatic precipitation, mass spectroscopy (Nuclear Magnetic Resonance) and MRI biomedical equipment (Magnetic Resonance Imaging) which are used to treat diseases. Magnetic fields are also necessary for the separation of metallic materials from non-metallic impurities. The third-grade fluid flow with MHD was investigated by Prasanth and Subba [6]. Hayat and Mehmood [7] explored the impact of slip on the MHD third-grade fluid flow in a planar pipe.

Peristalsis is a succession of muscle relaxation and vessel wall contraction that drives material ahead in fluids via tubes in a wave-like motion without having an interface with the parts of the pump. Peristaltic motion can be witnessed in the transit of food through the stomach, esophagus, and intestinal tract, blood through arteries, veins, and capillaries, urine through the ureter from the kidney to the bladder, and so on. Toxic liquids are transported in nuclear enterprises using the peristaltic phenomena. Additionally, engineers use the finger and roller pumps which run on the principle of peristalsis. Sanitary fluid transportation and other related applications. To circulate blood in the cardiovascular machine during surgery, osmotic motors are also used. The behaviour of a two-dimensional channel peristaltic pump was first examined by Latham [8]. The pulsatile flow of a viscous fluid was explored by Shapiro et al. [9]. Ever since, many initiatives to analyze the peristaltic transport phenomena under various hypotheses have been made (see a few studies [10–15]).

For industrial, medical, and technological applications, the flow of non-Newtonian and Newtonian fluids is preferable. The majority of fluids found in nature are non-Newtonian. Examples are tomato ketchup, blood, mud, honey, and other such fluids. The first researchers to examine the peristaltic flow of non-Newtonian fluids were Raju and Devanathan [16]. Mekheimer [17] investigated blood peristaltic flow in non-uniform channels. These flow issues are challenging to solve because of the highly nonlinear and sophistication of non-Newtonian fluids. A unique subclass of these fluids is termed third-grade fluid, associated with third-order truncation. The fluids of degree three include the fluids of grade three as a subclass. The first mathematical findings on fluids for third grade were reported by Amrouche and Cioranescu [18].

However, the citations only briefly address a few investigations on third-grade fluid [19–20]. The pulsatile flow of a third-grade fluid was then studied by Hayat et al. [21]. Haroun [22] looked at how Deborah's number and phase difference affected grade three fluid pulsatile transport. The third-order fluid flow in a tapered canal was researched by Prakash et al. [23]. Amin [24] studied a third-grade fluid's unsteady thin film fluid flow. Thermal radiation was utilized by Sridhar et al. [25] to describe the impact of mass and heat transfer on the peristalsis of Jeffrey fluid. Few references [26–30] related to the study of MHD, mixed convection, and radiation. Asha and Deepa [31] have investigated peristaltic flow alongside thermal radiation and entropy effects. Additionally, the impact of the MHD in a tapered canal was examined by Asha and Deepa [32]. Several studies on peristaltic flow are listed in the bibliography [33-35].

There is potential for chemical, engineering, and industrial applications of the current work. First, the pulsatile motion of a third-grade nanofluid through an asymmetric channel is examined to determine the effects of electro-osmotic transport, heat radiation, and magnetic field. We discovered that numerous scholars investigated peristaltic flow in various channels throughout the literature survey. However, no research has been done to show how the Adomian decomposition approach can be used on the electro-osmotic flow, radiation, and magnetic field. Finally, the graphs depicting the outcomes of various physical factors on concentration, temperature, velocity, heat-generation coefficient, and electro-osmotic coefficient are provided.

The present study holds potential for chemical, engineering, and industrial applications. First, the electro-osmotic transport, thermal radiation, and magnetic field are investigated in the peristaltic motion of third-grade nanofluid through an asymmetric channel. Throughout the literature review, we found that several researchers examined peristaltic flow in different channels. However, no study has been made to demonstrate the effect of electro-osmotic flow, radiation, and magnetic field in an asymmetric channel by the Adomian decomposition method. Finally, the impact of various physical parameters on temperature, concentration, velocity, heat generation coefficient, and electro-osmotic coefficient were graphically depicted.

2. MATHEMATICAL FORMUATION

We address the peristalsis of an immiscible third-order conducting nanofluid. A unified magnetic field is introduced to the flow in a perpendicular direction. By assuming that the fluid has poor electrical conductivity, the magnetic Reynolds number is taken to be modest, and the induced magnetic field is disregarded in favour of the applied magnetic field. The rectangular coordinate system is the one we select (\tilde{X}, \tilde{Y}) in which the X -axis is located near the channel's centreline and the Y -axis is perpendicular to it. Assume a wave train that is infinite and moves down the channel walls at c velocity. Figure 1 depicts a sketch of the channel.

The wall surfaces' geometry is represented by,

$$h_1(X, \tilde{t}) = d_1 + a_1 \cos\left[\frac{2\pi}{\lambda}(X - c\tilde{t})\right] - \text{Upper wall}, \tag{1}$$

$$h_2(X, \tilde{t}) = -d_2 - a_2 \cos\left[\frac{2\pi}{\lambda}(X - c\tilde{t}) + \phi\right] - \text{Lower wall}, \tag{2}$$

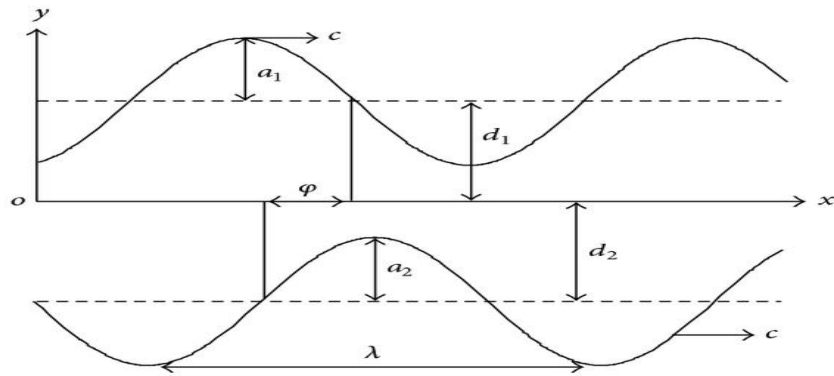


Figure1. A sketch of an asymmetric channel.

where $\phi(0 \leq \phi \leq \pi)$ is the phase difference, and a_1 and a_2 are the top wall's and lower wall's respective amplitudes. It is noted that $\phi = \pi$ corresponds to a symmetric channel with in-phase waves and $\phi = 0$ out-of-phase waves. \tilde{t} is the time, λ is the wavelength, d_1 and d_2 is the distance between the upper and lower wall's half-widths. V can be expressed as $V = [U(X, Y, \tilde{t}), V(X, Y, \tilde{t}), 0]$ where U and V are the velocities in X and Y direction in the stationary frame. Additionally, a_1, a_2, d_1 and d_2 satisfy the relation.

$$a_1^2 + a_2^2 + 2a_1a_2 \cos \phi \leq (d_1 + d_2)^2.$$

Electro-hydrodynamics:

The Poisson Eq. [26] is defined as

$$\nabla^2 \phi = -\frac{\rho_e}{\epsilon}, \tag{3}$$

here ϵ is the permittivity of dielectric, ρ_e is the overall density of charges, and ϕ is the electrical potential.

Potential distribution:

The entire charge density is distributed according to the Boltzmann distribution [27].

$$\rho_e = -z_v e (n^- - n^+). \tag{4}$$

The cations (n^+) and anions (n^-) are described by Boltzmann's equation.

$$n^\pm = n_0 e^{\left(\pm \frac{ezv}{T_{av} K_B}\right) \phi}, \tag{5}$$

where the electronic charge is e , the charge balance is z_v , the bulk concentration is n_0 , Boltzmann constant K_B and the average temperature is T_{av} .

As a result of Debye-Huckel linearisation [27]. Eq. (3) changes to

$$\frac{d^2\phi}{dy^2} = m_e^2\phi, \tag{6}$$

The electro-osmotic parameter is m_e and boundary conditions are $\phi = 1$ at $y = h_1$ and $\phi = -1$ at $y = -h_2$. Eq. (6) yields,

$$\phi(y) = \frac{\sinh[m_e(y+h)]}{\sinh[2hm_e]}. \tag{7}$$

The stress tensor model T for a third-order fluid is

$$T = -p\tilde{I} + S, \tag{8}$$

where \tilde{I} is the identity tensor, p is the pressure.

The extra stress tensor S is given by,

$$S = \mu A_1 + \alpha_1 A_2 + \alpha_2 A_2^2 + \beta_1 A_3 + \beta_2 (A_2 A_1 + A_1 A_2) + \beta_3 (tr A_1^2) A_1, \tag{9}$$

where the material constants $\mu, \alpha_1, \alpha_2, \beta_1, \beta_2$ and β_3 satisfy the condition $\mu \geq 0, \alpha_1 \geq 0, |\alpha_1 + \alpha_2| \leq \sqrt{24\mu\beta_3}, \beta_1 + \beta_2 = 0, \beta_2 \geq 0$.

The Rivlin- Ericksen tensor A_n are expressed by the relation

$$A_1 = (gradV) + (gradV)^T, \tag{10}$$

$$A_n = \frac{d}{dt} A_{n-1} + A_{n-1} (gradV) + (gradV)^T A_{n-1}, n \geq 1 \tag{11}$$

The governing Eqs. of mass, momentum, energy, and species concentration are stated as [7].

$$\frac{\partial \tilde{U}}{\partial \tilde{X}} + \frac{\partial \tilde{V}}{\partial \tilde{Y}} = 0, \tag{12}$$

$$\rho \left(\frac{\partial}{\partial \tilde{t}} + \tilde{U} \frac{\partial}{\partial \tilde{X}} + \tilde{V} \frac{\partial}{\partial \tilde{Y}} \right) \tilde{U} = -\frac{\partial \tilde{P}}{\partial \tilde{X}} + \left(\frac{\partial \tilde{S}_{\tilde{X}\tilde{X}}}{\partial \tilde{X}} + \frac{\partial \tilde{S}_{\tilde{X}\tilde{Y}}}{\partial \tilde{Y}} \right) + \rho_e E_x - \sigma B_0^2 \tilde{U} + \rho g k (\tilde{T} - T_0) + \rho g k' (\tilde{C} - C_0), \tag{13}$$

$$\rho \left(\frac{\partial}{\partial \tilde{t}} + \tilde{U} \frac{\partial}{\partial \tilde{X}} + \tilde{V} \frac{\partial}{\partial \tilde{Y}} \right) \tilde{V} = -\frac{\partial \tilde{P}}{\partial \tilde{Y}} + \left(\frac{\partial \tilde{S}_{\tilde{X}\tilde{X}}}{\partial \tilde{X}} + \frac{\partial \tilde{S}_{\tilde{Y}\tilde{Y}}}{\partial \tilde{Y}} \right), \tag{14}$$

$$\rho C_p \left(\frac{\partial}{\partial \tilde{t}} + \tilde{U} \frac{\partial}{\partial \tilde{X}} + \tilde{V} \frac{\partial}{\partial \tilde{Y}} \right) \tilde{T} = K \left[\frac{\partial^2}{\partial \tilde{X}^2} + \frac{\partial^2}{\partial \tilde{Y}^2} \right] \tilde{T} + \left(\frac{\partial \tilde{U}}{\partial \tilde{X}} \tilde{S}_{\tilde{X}\tilde{X}} + \frac{\partial \tilde{V}}{\partial \tilde{Y}} \tilde{S}_{\tilde{Y}\tilde{Y}} + \left(\frac{\partial \tilde{U}}{\partial \tilde{X}} + \frac{\partial \tilde{V}}{\partial \tilde{Y}} \right) \tilde{S}_{\tilde{X}\tilde{Y}} \right) - \frac{\partial q_r}{\partial \tilde{Y}}, \tag{15}$$

$$\left(\frac{\partial}{\partial \tilde{t}} + \tilde{U} \frac{\partial}{\partial \tilde{X}} + \tilde{V} \frac{\partial}{\partial \tilde{Y}}\right) \tilde{C} = D_m \left[\frac{\partial^2}{\partial \tilde{X}^2} + \frac{\partial^2}{\partial \tilde{Y}^2}\right] \tilde{C} + \frac{k_t D_m}{T_m} \left[\frac{\partial^2}{\partial \tilde{X}^2} + \frac{\partial^2}{\partial \tilde{Y}^2}\right] \tilde{T}. \tag{16}$$

where ρ_e is the electric charge density, ρ is the fluid density, E_x is the axial electric field, P is the pressure, σ is the electrical conductivity, k is the thermal expansion coefficient, g is the acceleration due to gravity, k' is the concentration expansion co-efficient., q_r is the radiative heat flux, k_t is the thermal diffusion, D_m is the mass diffusivity, T_m is the average temperature, \tilde{T} and \tilde{C} are the non-dimensional temperature and species concentration, respectively.

Thermal radiation

The Rosseland approximation and diffusion approximation can be used to define the radiative flux q_r as

$$q_r = -\frac{4\sigma_1}{3k_1} \frac{\partial \tilde{T}^4}{\partial \tilde{Y}}, \tag{17}$$

$$\frac{\partial q_r}{\partial \tilde{y}} = -\frac{16\sigma_1}{3k_1} \tilde{T}^4 \frac{\partial^2 \tilde{T}^4}{\partial \tilde{Y}^2}. \tag{18}$$

By utilising Taylor's series to expand \tilde{T}^4 about T_0 and ignoring higher-order terms, assuming that temperature variances are small enough to allow for \tilde{T}^4 to be represented as

$$\begin{aligned} \tilde{T}^4 &\approx T_0^4 + 4T_0^3 (\tilde{T} - T_0), \\ \tilde{T}^4 &\approx -3T_0^4 + 4T_0^3 \tilde{T}, \end{aligned} \tag{19}$$

$$\frac{\partial q_r}{\partial \tilde{y}} = -\frac{16\sigma_1}{3k_1} T_0^3 \frac{\partial^2 \tilde{T}^4}{\partial \tilde{Y}^2}. \tag{20}$$

Using this in Eq. (15) we have,

$$\begin{aligned} \rho C_p \left(\frac{\partial}{\partial \tilde{t}} + \tilde{U} \frac{\partial}{\partial \tilde{X}} + \tilde{V} \frac{\partial}{\partial \tilde{Y}}\right) \tilde{T} &= K \left[\frac{\partial^2}{\partial \tilde{X}^2} + \frac{\partial^2}{\partial \tilde{Y}^2}\right] \tilde{T} + \left(\frac{\partial \tilde{U}}{\partial \tilde{X}} \tilde{S}_{\tilde{x}\tilde{x}} + \frac{\partial \tilde{V}}{\partial \tilde{Y}} \tilde{S}_{\tilde{y}\tilde{y}} + \left(\frac{\partial \tilde{U}}{\partial \tilde{X}} + \frac{\partial \tilde{V}}{\partial \tilde{Y}}\right) \tilde{S}_{\tilde{x}\tilde{y}}\right) \\ &\quad + \frac{16\sigma_1}{3k_1} T_0^3 \frac{\partial^2 \tilde{T}^4}{\partial \tilde{Y}^2}. \end{aligned} \tag{21}$$

We analyze the following transformations between the steady stationary frame (\tilde{X}, \tilde{Y}) and the unsteady moving frame (\tilde{x}, \tilde{y}) [29],

$$\begin{aligned} \tilde{x} &= \tilde{X} - c\tilde{t}, \quad \tilde{y} = \tilde{Y}, \quad \tilde{v}(\tilde{x}, \tilde{y}) = \tilde{V}(\tilde{X}, Y\tilde{t}), \quad \tilde{u}(\tilde{x}, \tilde{y}) = \tilde{U}(\tilde{X}, Y\tilde{t}) - c, \quad \tilde{t}(\tilde{x}, \tilde{y}) = \tilde{T}(\tilde{X}, \tilde{Y}, \tilde{t}) \\ \tilde{p}(\tilde{x}, \tilde{y}) &= \tilde{P}(\tilde{X}, \tilde{Y}, \tilde{t}), \end{aligned} \tag{22}$$

Employing the transformations in Eqs. (12) to (14), (16) and (21) we implement the dimensionless quantities listed below;

$$\begin{aligned}
 x &= \frac{2\pi\tilde{x}}{\lambda}, y = \frac{\tilde{y}}{a}, t = \frac{2\pi c\tilde{t}}{\lambda}, u = \frac{\bar{u}}{c}, v = \frac{\bar{v}}{c}, p = \frac{2\pi a^2}{\lambda c\mu} \tilde{p}, \alpha = \frac{2\pi a}{\lambda}, h = \frac{\tilde{h}}{a}, P_e = \frac{C\lambda}{D}, m_e = \frac{a}{\lambda D}, \\
 n &= \frac{\tilde{n}}{n_0}, \tilde{n} = \frac{b}{a}, \theta = \frac{\tilde{T} - T_0}{T_0}, \phi = \frac{\tilde{C} - C_0}{C_0}, \lambda_D = \frac{1}{ez_v} \sqrt{\frac{T_0 \tilde{n} K_B}{2n_0}}, E_c = \frac{c^2}{c_p T_0}, \varnothing = \frac{ez_v}{T_{av} K_B} \tilde{\varnothing}, U_{hs} = -\frac{E_x \tilde{n}}{c\mu} \\
 S &= \frac{a}{c\mu} \tilde{S}, \lambda_1 = \frac{a_1 c}{a\mu}, \lambda_2 = \frac{a_2 c}{a\mu}, \gamma_1 = \frac{\beta_1 c^2}{\alpha^2 \mu}, \gamma_2 = \frac{\beta_2 c^2}{\alpha^2 \mu}, \gamma_3 = \frac{\beta_3 c^2}{\alpha^2 \mu}, \Gamma = \gamma_3 + \gamma_2, S_c = \frac{\mu}{\rho D_m}, \\
 S_r &= \frac{\rho D_m K_T T_0}{\mu T_m C_0}, G_r = \frac{\rho g B_T T_0 a^2}{c\mu}, G_c = \frac{\rho g B_c C_0 a^2}{c\mu}, R_n = \frac{16\sigma_1}{3c_p \mu k_1} T_0^3, M^2 = \frac{\sigma a^2 B_0^2}{\mu}, \psi = \frac{\tilde{\psi}}{ca}, u = \frac{\partial \psi}{\partial y}, \\
 v &= -\alpha \frac{\partial \psi}{\partial x}, Re = \frac{\rho c a}{\mu}, P_r = \frac{\mu c_p}{k}, B_r = E_c P_r, F = \frac{\tilde{q}}{ca}, \Theta = \frac{\tilde{Q}}{ca}. \tag{23}
 \end{aligned}$$

In view of (23), Eqs. (13)-(15) and (21) become,

$$Re\alpha \left[\frac{\partial \psi}{\partial y} \frac{\partial}{\partial x} - \frac{\partial \psi}{\partial y} \frac{\partial}{\partial y} \right] \frac{\partial \psi}{\partial y} = -\frac{\partial p}{\partial x} + \left(\alpha \frac{\partial S_{xx}}{\partial x} + \frac{\partial S_{xy}}{\partial y} \right) + m_e^2 U_{hs} \varnothing - M^2 \left(\frac{\partial \psi}{\partial y} + 1 \right) + G_r \theta + G_c \phi, \tag{24}$$

$$-Re\alpha^3 \left[\frac{\partial \psi}{\partial y} \frac{\partial}{\partial x} - \frac{\partial \psi}{\partial y} \frac{\partial}{\partial y} \right] \frac{\partial \psi}{\partial x} = -\frac{\partial P}{\partial y} + \alpha \left(\alpha \frac{\partial S_{xx}}{\partial x} + \frac{\partial S_{xy}}{\partial y} \right), \tag{25}$$

$$\begin{aligned}
 Re\alpha \left[\frac{\partial \psi}{\partial y} \frac{\partial}{\partial x} - \frac{\partial \psi}{\partial y} \frac{\partial}{\partial y} \right] \theta &= \frac{1}{P_r} \left(\alpha^2 \frac{\partial^2}{\partial x^2} + \frac{\partial^2}{\partial y^2} \right) \theta + E_c \left[\alpha^2 \frac{\partial}{\partial x} \left(\frac{\partial \psi}{\partial x} \right) S_{xx} - \alpha \frac{\partial}{\partial y} \left(\frac{\partial \psi}{\partial x} \right) S_{yy} + \left(\frac{\partial^2 \psi}{\partial y^2} - \alpha^2 \frac{\partial^2 \psi}{\partial x^2} \right) S_{xy} \right] + \\
 &R_n \frac{\partial^2 \theta}{\partial y^2}, \tag{26}
 \end{aligned}$$

$$Re\alpha \left[\frac{\partial \psi}{\partial y} \frac{\partial}{\partial x} - \frac{\partial \psi}{\partial y} \frac{\partial}{\partial y} \right] \Omega = \frac{1}{S_c} \left(\alpha^2 \frac{\partial^2}{\partial x^2} + \frac{\partial^2}{\partial y^2} \right) \Omega + S_r \left(\alpha^2 \frac{\partial^2}{\partial x^2} + \frac{\partial^2}{\partial y^2} \right) \theta. \tag{27}$$

Utilising the low Reynolds number and long wavelength approximations for Eqs. (24)-(27) and omitting higher order terms of the result, we arrive at

$$\frac{\partial p}{\partial x} = \frac{\partial (S_{xy})}{\partial x} + m_e^2 U_{hs} \varnothing - M^2 \left(\frac{\partial \psi}{\partial y} + 1 \right) + G_r \theta + G_c \phi = 0, \tag{28}$$

$$\frac{\partial p}{\partial y} = 0, \tag{29}$$

$$\frac{\partial^2 \theta}{\partial y^2} (1 + R_n P_r) + B_r [S_{xy}] \frac{\partial^2 \psi}{\partial y^2} = 0, \tag{30}$$

$$\frac{\partial^2 \Omega}{\partial y^2} + S_c S_r \left(\frac{\partial^2 \theta}{\partial y^2} \right) = 0. \tag{31}$$

Omitting pressure from Eqs. (28) and (29), we obtain

$$\frac{\partial^2 (S_{xy})}{\partial y^2} + m_e^2 U_{hs} \phi - M^2 \left(\frac{\partial^2 \psi}{\partial y^2} \right) + G_r \frac{\partial \theta}{\partial y} + G_c \frac{\partial \phi}{\partial y} = 0, \tag{32}$$

where $S_{xy} = \frac{\partial^2 \psi}{\partial y^2} + 2\Gamma \left(\frac{\partial^2 \psi}{\partial y^2} \right)^3$.

The non-dimensional boundary conditions are,

$$\psi = \frac{F}{2}, \frac{\partial \psi}{\partial y} = 0, \theta = 0, \phi = 0, \quad \text{at } y = h_1 \tag{33}$$

$$\psi = -\frac{F}{2}, \frac{\partial \psi}{\partial y} = 0, \theta = 1, \phi = 1, \quad \text{at } y = h_2$$

The non-dimensional mean flow rate F in the moving frame and fixed frame are related by,

$$\Theta = F + 1, \tag{34}$$

where, $F = \int_{-h_1}^{h_2} \frac{\partial \psi}{\partial y} dy = \psi [h_1(x)] + \psi [-h_2(x)]$.

The non-dimensional heat transfer co-efficient is given by,

$$Z = h_x \left| \frac{\partial \theta}{\partial y} \right|. \tag{35}$$

3. METHOD OF SOLUTION

The nonlinear system of the preceding Eqs. (28)–(31) with the boundary conditions (33) are solved by employing the Adomian decomposition method. Double integration of Eq. (31) yields

$$\theta = c_1 e^{s_1 y} + c_2 e^{-s_1 y}, \tag{36}$$

Using the above Eq. (36) in Eq. (30), we get,

$$\Omega = \frac{-(S_c S_r)(e^{-s_1 h_1} e^{s_1 y} + e^{s_1 h_1} e^{-s_1 y})}{(e^{s_1 h_1} e^{s_1 h_2} - e^{s_1 h_1} e^{-s_1 h_2})} - c_3 y - c_4, \tag{37}$$

where $s_1 = \sqrt{\frac{QP_r}{(1+N_r)}}$.

Utilising the suitable boundary conditions of Eq. (33), we obtain,

$$c_1 = \frac{e^{s_1 h_2}}{(e^{-s_1(h_1-h_2)} - e^{s_1(h_1-h_2)})e^{s_1(h_1+h_2)}}, \text{ and } c_2 = \frac{e^{s_1 h_1}}{(e^{-s_1(h_1-h_2)} - e^{s_1(h_1-h_2)})},$$

$$c_3 = -\frac{1}{(h_2 - h_1)} - \frac{(S_c S_r)}{(e^{s_1 h_1} e^{s_1 h_2} - e^{s_1 h_1} e^{-s_1 h_2})(h_2 - h_1)} \left[\frac{e^{-s_1 h_1} e^{s_1 h_2} + e^{s_1 h_1} e^{-s_1 h_2}}{h_2^2} - \frac{e^{-s_1 h_1} e^{s_1 h_1} + e^{s_1 h_1} e^{-s_1 h_1}}{h_1^2} \right],$$

$$c_4 = \frac{(S_c S_r)(e^{-s_1 h_1} e^{s_1 h_1} + e^{s_1 h_1} e^{-s_1 h_1})}{(e^{s_1 h_1} e^{s_1 h_2} - e^{s_1 h_1} e^{-s_1 h_2})} + \frac{h_1}{(h_2 - h_1)} + \frac{(S_c S_r)}{(e^{s_1 h_1} e^{s_1 h_2} - e^{s_1 h_1} e^{-s_1 h_2})(h_2 - h_1)} \left[\frac{e^{-s_1 h_1} e^{s_1 h_2} + e^{s_1 h_1} e^{-s_1 h_2}}{h_2^2} - \frac{e^{-s_1 h_1} e^{s_1 h_1} + e^{s_1 h_1} e^{-s_1 h_1}}{h_1^2} \right].$$

The Adomian Decomposition Method (ADM) is implemented to solve Eq. (28) in the following manner;

$$L_{yyy} [\psi] - n^2 [\psi_y] = \frac{\partial p}{\partial x} / 2\Gamma + n^2 - \frac{\partial^2}{\partial y^2} [\psi_{yyy}]^3 - \frac{G_t}{2\Gamma} \theta - \frac{G_c}{2\Gamma} \phi, \tag{38}$$

where $n^2 = M^2$.

The inverse operator $L_{yyy}^{-1} = \iiint [\cdot] dy dy dy$ can be used to write Eq. (5.27) as,

$$\psi = \frac{1}{2\Gamma} \left(c_1 + c_2 y + c_3 \frac{y^2}{2!} \right) + \frac{1}{2\Gamma} L_{yyy}^{-1} \left[\frac{\partial p}{\partial x} + n^2 \right] + \frac{1}{2\Gamma} L_{yyy}^{-1} [n^2 \psi_y] - L_{yyy}^{-1} \left[\frac{\partial^2}{\partial y^2} [\psi_{yy}]^3 \right] - \frac{G_t}{2\Gamma} L_{yyy}^{-1} [\theta] - \frac{G_c}{2\Gamma} L_{yyy}^{-1} [\phi]. \tag{39}$$

We now decompose ψ as $\psi = \sum_{n=0}^{\infty} \psi_n$, where $n \geq 0$ (40)

$$\psi_0 = \frac{1}{2\Gamma} \left(A_1 + A_2 y + A_3 \frac{y^2}{2!} \right) + \frac{1}{2\Gamma} \left\{ \left(\frac{\partial p}{\partial x} + n^2 \right) - Gtc_3 + Gc \left(SrSc + \frac{N_t}{N_b} \right) c_3 + Gcc_2 \right\} \frac{y^3}{3!} + \frac{1}{2\Gamma} \left\{ Gcc_4 \left(SrSc + \frac{N_t}{N_b} \right) - Gtc_4 \right\} \frac{e^{Cy}}{y^3} + \frac{1}{2\Gamma} Gcc_1 \frac{y^4}{4!}, \tag{41}$$

$$\psi_{n+1} = \iiint \left[\frac{n^2}{2\Gamma} (\psi_n)_y \right] dy dy dy - \iiint \frac{\partial^2}{\partial y^2} [(\psi_n)_{yy}]^3. \text{ where } n \geq 0$$

Therefore,

$$\psi_1 = k^2 \left[A_2 \frac{y^3}{3!} + A_3 \frac{y^4}{4!} + \left\{ \left(\frac{\partial p}{\partial x} + n^2 \right) - Gtc_3 + Gc \left(SrSc + \frac{N_t}{N_b} \right) c_3 + Gcc_2 \right\} \frac{y^5}{5!} + \left\{ Gcc_4 \left(SrSc + \frac{N_t}{N_b} \right) - Gtc_4 \right\} \frac{e^{Cy}}{y^3} + Gcc_1 \frac{y^6}{6!} \right],$$

$$\psi_2 = k^4 \left[A_2 \frac{y^5}{5!} + A_3 \frac{y^6}{6!} + \left\{ \left(\frac{\partial p}{\partial x} + n^2 \right) - Gtc_3 + Gc \left(SrSc + \frac{N_t}{N_b} \right) c_3 + Gcc_2 \right\} \frac{y^7}{7!} + \left\{ Gcc_4 \left(SrSc + \frac{N_t}{N_b} \right) - Gtc_4 \right\} \frac{e^{Cy}}{y^7} + Gcc_1 \frac{y^8}{8!} \right],$$

$$\psi_n = k^{2n} \left[A_2 \frac{y^{2n+1}}{(2n+1)!} + A_3 \frac{y^{2n+2}}{(2n+2)!} + \left\{ \left(\frac{\partial p}{\partial x} + n^2 \right) - Gtc_3 + Gc \left(SrSc + \frac{N_t}{N_b} \right) c_3 + Gcc_2 \right\} \frac{y^{2n+3}}{(2n+3)!} + \left\{ Gcc_4 \left(SrSc + \frac{N_t}{N_b} \right) - Gtc_4 \right\} \frac{e^{Cy}}{y^{2n+3}} + Gcc_1 \frac{y^{2n+4}}{(2n+4)!} \right].$$

where $k = \left(\frac{n}{2\Gamma} \right)^2$.

The analytical solution of ψ can be expressed as follows, according to Eq. (40)

$$\psi = \frac{A_1}{2\Gamma} + \left[\frac{A_2}{k} \sinh(ky) + \frac{A_3}{k^2} (\cosh(ky) - 1) \right] \left\{ \left(\frac{\partial p}{\partial x} + n^2 \right) - Gtc_3 + Gcc_3 \left(SrSc + \frac{N_t}{N_b} \right) + Gcc_2 \right\} \frac{1}{k^3} (\sinh(ky) - ky) \text{ which can be} \\ + \left[Gcc_4 \left(SrSc + \frac{N_t}{N_b} \right) - Gtc_4 \right] \frac{e^{Cy}}{Ck^2} + \frac{Gcc_1}{k^4} \left[\cosh(ky) - 1 - \frac{(ky)^2}{2!} \right],$$

simplified as,

$$\psi = F_1 + F_2 \sinh(ky) + F_3 \cosh(ky) + e^{Cy} \cosh(ky). \tag{42}$$

where

$$F_1 = \frac{F}{4\Gamma} - \left[\frac{A_2}{k} \sinh(kh_1) + \frac{A_3}{k^2} (\cosh(kh_1) - 1) \right] \left\{ \left(\frac{\partial p}{\partial x} + n^2 \right) - Gtc_3 + Gcc_3 \left(SrSc + \frac{N_t}{N_b} \right) + Gcc_2 \right\} \frac{1}{k^3} (\sinh(kh_1) - kh_1) \\ + \left[Gcc_4 \left(SrSc + \frac{N_t}{N_b} \right) - Gtc_4 \right] \frac{e^{Ch_1}}{Ck^2} + \frac{Gcc_1}{k^4} \left[\cosh(kh_1) - 1 - \frac{(kh_1)^2}{2!} \right],$$

$$\begin{aligned}
 F_2 = & \frac{-\tanh(kh_2)}{\sinh[k(h_1+h_2)]} + \left[\left\{ \left(\frac{\partial p}{\partial x} + n^2 \right) - Gtc_3 + Gcc_3 \left(SrSc + \frac{N_t}{N_b} \right) + Gcc_2 \right\} \left(\frac{\cosh(kh_1-1)\cosh(kh_2)}{k^2} \right. \right. \\
 & \left. \left. - \frac{\cosh(kh_1-1)\cosh(kh_2)}{k^2} \right) \right] + \left\{ Gcc_4 \left(SrSc + \frac{N_t}{N_b} \right) - Gtc_4 \right\} \left(\frac{e^{Ch_1}\cosh(kh_2)}{k^2} - \frac{e^{Ch_2}\cosh(kh_1)}{k^2} \right) + \\
 & \frac{Gcc_1}{k^3} \left(\{\sinh(kh_2) + kh_2\} \cosh(kh_1) - \{\sinh(kh_1) + kh_1\} \cosh(kh_2) \right) + \left\{ \left(\frac{\partial p}{\partial x} + n^2 \right) - Gtc_3 + \right. \\
 & \left. Gcc_3 \left(SrSc + \frac{N_t}{N_b} \right) + Gcc_2 \right\} \frac{\cosh(kh_2-1)\cosh(kh_1)}{k^2} - \frac{Gcc_1}{k^3} \{\sinh(kh_2) + kh_2\} \cosh(kh_1), \\
 F_3 = & \frac{-k}{\sinh[k(h_1+h_2)]} \left\{ \left(\frac{\partial p}{\partial x} + n^2 \right) - Gtc_3 + Gcc_3 \left(SrSc + \frac{N_t}{N_b} \right) + Gcc_2 \right\} \left(\frac{\cosh(kh_1-1)\cosh(kh_2)}{k^2} \right. \\
 & \left. - \frac{\cosh(kh_2-1)\cosh(kh_1)}{k^2} \right) + \left\{ Gcc_4 \left(SrSc + \frac{N_t}{N_b} \right) - Gtc_4 \right\} \left(\frac{e^{Ch_1}\cosh(kh_2)}{k^2} - \frac{e^{Ch_2}\cosh(kh_1)}{k^2} \right) + \\
 & \frac{Gcc_1}{k^3} \left(\{\sinh(kh_2) + kh_2\} \cosh(kh_1) - \{\sinh(kh_1) + kh_1\} \cosh(kh_2) \right).
 \end{aligned}$$

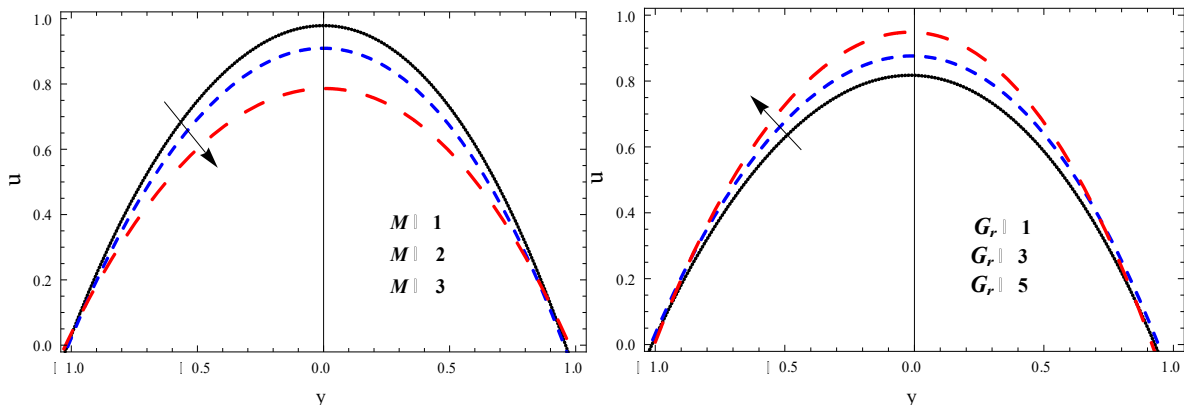
The velocity expression is provided by

$$\begin{aligned}
 u = & A_2 \cosh(ky) - \frac{A_3}{k} \sinh(ky) + \left\{ \left(\frac{\partial p}{\partial x} + n^2 \right) - Gtc_3 + Gcc_3 \left(SrSc + \frac{N_t}{N_b} \right) + Gcc_2 \right\} \frac{\cosh(ky-1)}{k^2} + \\
 & \left\{ Gcc_4 \left(SrSc + \frac{N_t}{N_b} \right) - Gtc_4 \right\} \frac{e^{Cy}}{k^2} - \frac{Gcc_1}{k^3} \{\sinh(ky) + ky\}. \tag{43}
 \end{aligned}$$

4. RESULTS AND DISCUSSION

The impacts of various physical parameters are discussed, such as magnetic field parameter M , Grashoff number G_r , Species concentration Grashoff number G_c , Deborah number Γ , electro-osmotic parameter m_e , Schmidt number S_c , Soret number S_r , Brinkmann number B_r and thermal radiation parameter R_n on temperature, velocity, concentration, and heat transfer coefficient are discussed in this section.

4.1. Effect of axial velocity for (a) magnetic field parameter M , (b) Grashoff number G_r , (c) Species concentration Grashoff number G_c , (d) Deborah number Γ , (e) electro-osmotic parameter m_e (For asymmetric channel)



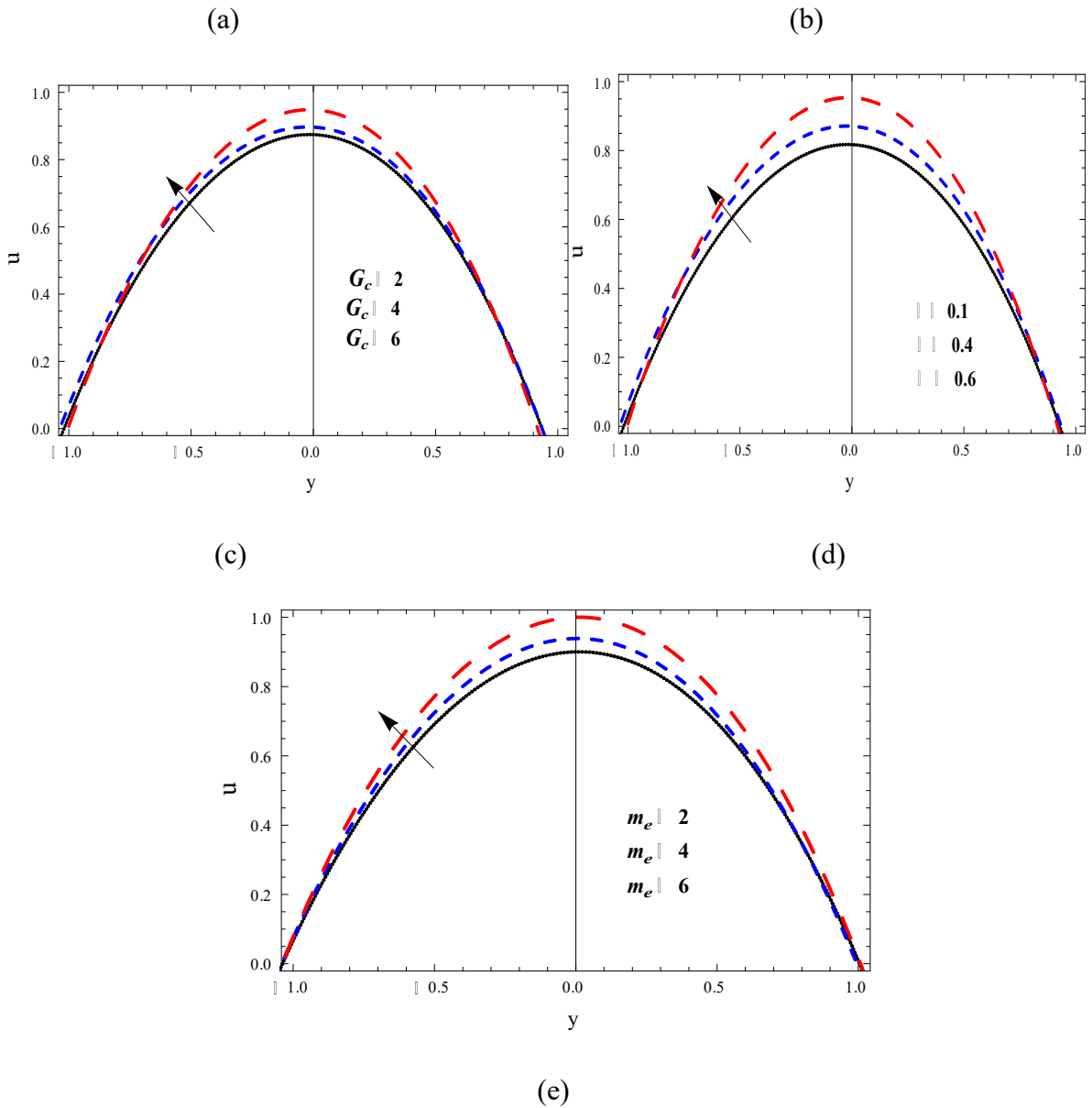


Figure 2. Velocity profile (u) for (a) M (b) G_r (c) G_c (d) Γ (e) m_e , while other parameters are $x = 0.2, U = -2, m_e = 2, B_r = 2, \Gamma = 0.01, M = G_r = S_c = S_r = R_n = P_r = 1, G_c = 0.2, \Theta = 1.8$.

Figure 2 describes the velocity profile for various parameters such as magnetic field parameter $M(1 \leq M \leq 3)$, the temperature Grashoff number $G_r(1 \leq G_r \leq 5)$, the concentration Grashoff number $G_c(2 \leq G_c \leq 6)$, Deborah number $\Gamma(0.1 \leq \Gamma \leq 0.6)$ and electro-osmotic parameter $m_e(2 \leq m_e \leq 6)$. In figure 2 (a), it can be observed that a higher value of M decreases the velocity. This is because of the Lorentz forces. Figure 2 (b) depicts that an increase in G_r enhances velocity. This is because as velocity increases, the buoyant forces increase. Figure 2 (c) shows a similar effect, where as G_c grows, the left wall velocity and right wall velocity increases. Figure 2 (d) demonstrates that as Γ rises, the velocity u increases at the centre of the channel and near the channel walls. In Figure 2 (e), we observe that the magnitude of u is enhanced near the walls of the channel as m_e increases. The reason for this is as m_e increases, the effect of the electric field increases which accelerates the fluid particles and hence enhances the velocity.

4.1.1. Effect of axial velocity for (a) Deborah number Γ (b) electro-osmotic parameter m_e (for symmetric channel)

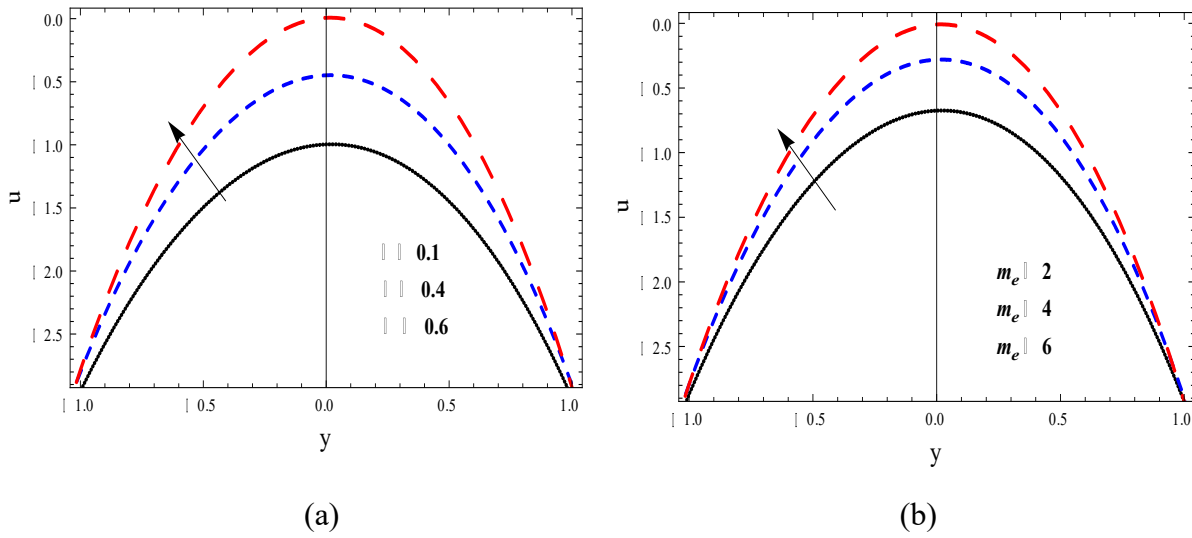
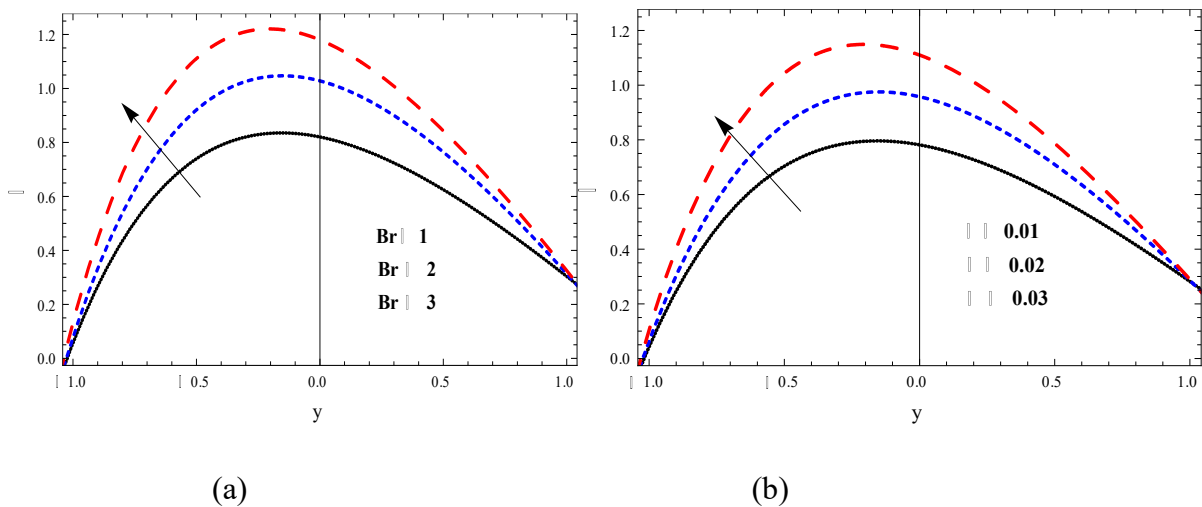


Figure 2.1. Velocity profile (u) for (a) M (b) G_r (c) G_c (d) Γ (e) m_e , while other parameters are $x = 0.2, U = -2, m_e = 2, B_r = 2, \Gamma = 0.01, M = G_r = S_c = S_r = R_n = P_r = 1, G_c = 0.2, \Theta = 1.8$

Figures 2.1.(a) and (b) depict the velocity profile for Deborah number Γ and electro-osmotic parameter m_e (for symmetric channel). It is observed that both Deborah number Γ and electro-osmotic parameter m_e enhance the velocity profile. Similar results are obtained in Fig. 2(d) and (e) for a asymmetric channel. It is observed from fig. 2(d) and 2.1(a) that, as the electro-osmotic parameter m_e increases from $m_e = 2, 4, 6$, the magnitude of velocity for an asymmetric channel increases by 25% approximately (see fig. 2(d)) whereas the magnitude of velocity for a symmetric channel increases by 95% approximately (see fig. 2.1 (a)). Similarly, it is observed from fig. 2(e) and 2.1(b) that as Deborah number Γ increases, the magnitude of velocity for an asymmetric channel increases by 20% approximately (see fig. 2(e)) whereas the magnitude of velocity for a symmetric channel increases by 63% approximately (see fig. 2.1 (b)).

4.2. Effect of Temperature for different parameters, such as Brinkman number B_r , electro-osmotic parameter m_e , Deborah number Γ and thermal radiation parameter R_n .



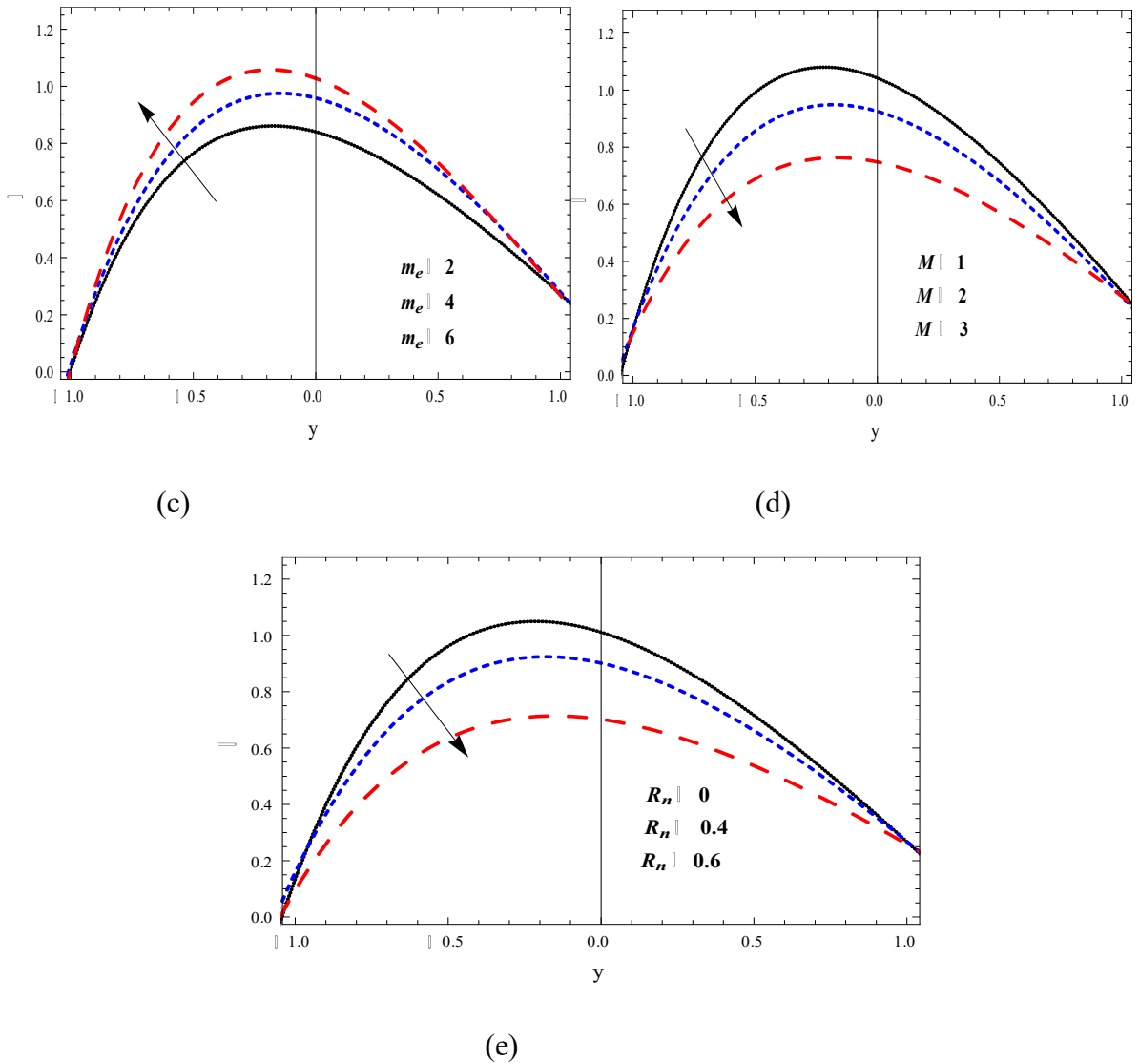


Figure 3. Temperature (θ) for (a) B_r (b) Γ (c) m_e (d) M (e) γ (f) R_n , while other parameters are $x = 0.2, U = -2, m_e = 2, B_r = 2, \Gamma = 0.01, M = G_r = S_c = S_r = R_n = P_r = 1, G_c = 0.2, \Theta = 1.8$

Figure 3 encases the temperature profile θ for different parameters such as Brinkman number B_r ($1 \leq B_r \leq 5$), electro-osmotic parameter m_e ($2 \leq m_e \leq 6$), magnetic field parameter M ($1 \leq M \leq 3$), Deborah number Γ ($0.1 \leq \Gamma \leq 0.6$) and thermal radiation parameter R_n ($0.0 \leq R_n \leq 0.6$) respectively. Figure 3(a) shows how an increase in B_r enhances fluid temperature because it reflects viscous dissipation or the conversion of kinetic energy to internal energy in response to viscosity. Figure 3(b) reveals that the temperature profile θ is enhanced as Γ increases. This is because Deborah number characterizes the fluidity of materials under certain flow conditions. As Deborah number enhances, there is a deformity in the fluid particles which enhances the temperature. Figure 3(c) shows that as θ increases, the fluid particles get charged and leads to higher values of m_e , whereas the temperature θ reduces for higher M as seen in Figure 3(d). Figure 3(e) depicts that the temperature is decelerated by enhancing R_n .

4.3. Concentration profile for various parameters such as Deborah number Γ , electro-osmotic parameter m_e , Schmidt number S_c , Soret number S_r , Brinkmann number B_r

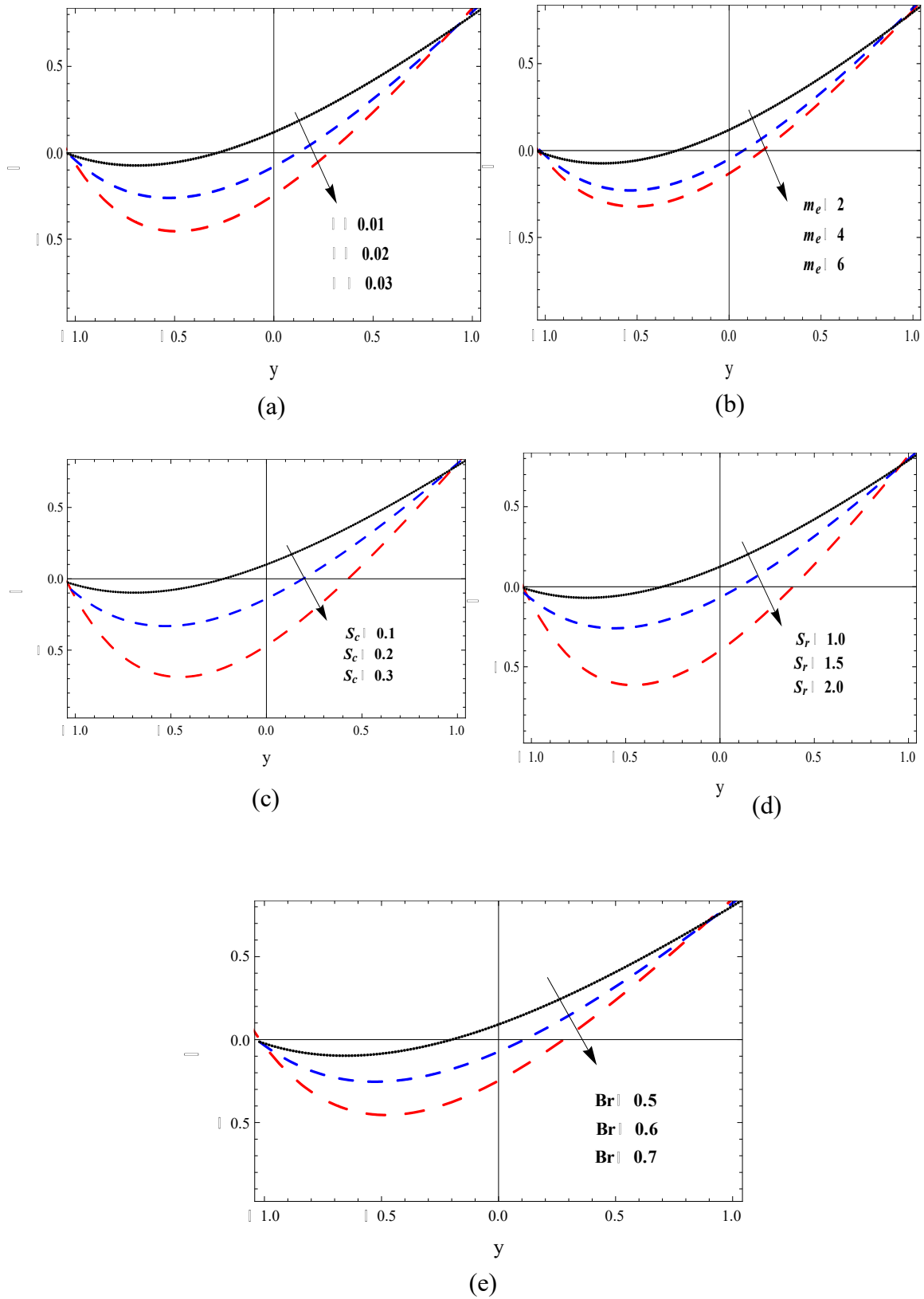
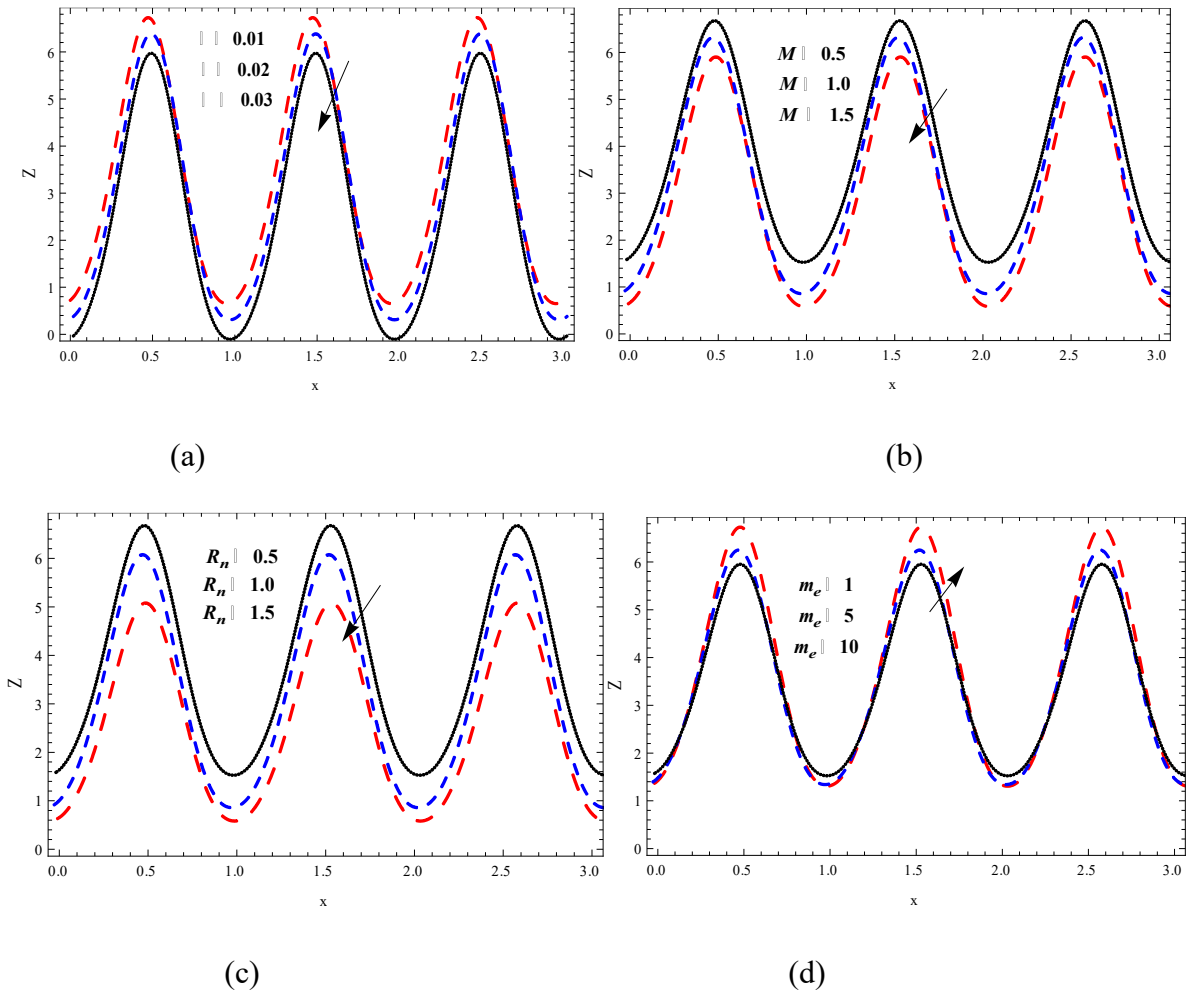
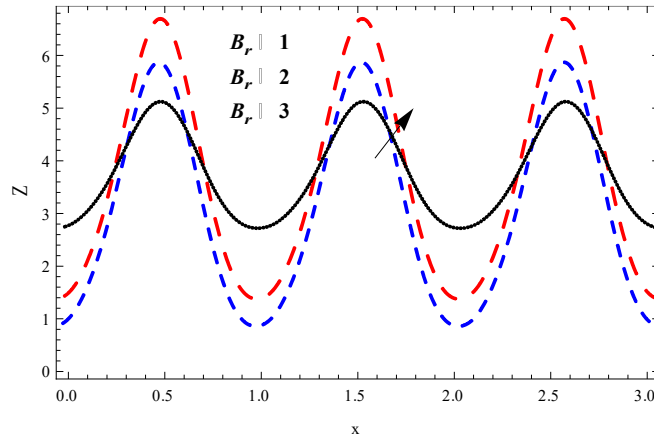


Figure 4. Concentration (ϕ) for (a) Γ (b) m_e (c) S_r (d) S_c (e) B_r , while other parameters are $x = 0.2, U = -2, m_e = 2, B_r = 2, \Gamma = 0.01, M = G_r = S_c = S_r = R_n = P_r = 1, G_c = 0.2, \Theta = 1.8$

Figure 4 explains the concentration profile for diverse parameters such as Deborah number Γ ($0.1 \leq \Gamma \leq 0.6$), electro-osmotic parameter m_e ($2 \leq m_e \leq 6$), Schmidt number S_c ($0.1 \leq S_c \leq 0.3$), Soret number S_r ($1 \leq S_r \leq 2$) and Brinkmann number B_r ($0.5 \leq B_r \leq .7$). Figure 4(a) shows that higher values of Γ decrease ϕ . It is because of the deformity caused for higher values Γ . Figure 4(b) manifests that ϕ reduces for higher values of m_e . As m_e increases there is a migration of the fluid molecules which reduces the concentration. Figure 4(c) intimates that ϕ is decelerated for more values of S_c . Since Schmidt's number is the ratio of kinematic viscosity to mass diffusivity, As S_c increases, there is a decrease in the mass diffusivity, which reduces the concentration. A similar result is obtained in Figure 4(d) for different values of S_r . Figure 4(e) expresses that ϕ decreases for higher values of B_r . This behaviour is due to the slower the conduction of heat produced by viscous dissipation with an increase in B_r and hence the lowers the concentration profile.

4.4. Impact of Heat transfer co-efficient for different parameters such as Deborah number Γ , magnetic field parameter M , thermal radiation parameter R_n , electro-osmotic parameter m_e and Brinkmann number B_r .





(e)

Figure 5. Heat transfer co-efficient (z) for (a) Γ (b) M (c) R_n (d) m_e (e) B_r , while other parameters are $x = 0.2, U = -2, m_e = 2, B_r = 2, \Gamma = 0.01, M = G_r = S_c = S_r = R_n = P_r = 0.5, G_c = 0.2, \Theta = 2$

Figure 5 illustrates the impact of heat transfer co-efficient Z for various values of Deborah number Γ ($0 \leq \Gamma \leq 0.4$), magnetic field parameter M ($1 \leq M \leq 3$), thermal radiation parameter R_n ($0.0 \leq R_n \leq 0.6$), electro-osmotic parameter m_e ($1 \leq m_e \leq 10$) and Brinkmann number B_r ($1.0 \leq B_r \leq 3.0$). Figure 5(a) shows that the heat transfer Z decreases with the increase in Γ because the difference in temperature between a solid surface and surrounding fluid decreases for higher values of Γ leading to a decrease in the heat transfer co-efficient. Similar behaviour is shown in the case of magnetic field parameter M and thermal radiation parameter R_n as depicted in Figure 5 (b) and (c) respectively. From Figure 4(d), it is observed that an increase in the electro-osmotic parameter m_e enhances the mobility of the fluid particles, which increases the heat transfer rate. Figure 4(e) shows that the heat transfer coefficient rises with an increase in B_r . This is because Brinkmann number signifies the ratio of viscous heat generation to external heating. The higher its value, the slower the conduction of heat produced by viscous dissipation, and hence the larger the heat transfer co-efficient.

Comparison of the velocity profile (u) for m_e , while other parameters are $x = 0.2, U = -2, m_e = 2, B_r = 2, \Gamma = 0.01, M = G_r = S_c = S_r = R_n = P_r = 1, G_c = 0.2, \Theta = 1.8$.

y	Tanveer et al. [35]	Current work
-1.0	-0.01158	-0.01158
-0.5	-0.01675	-0.01677
0.0	-0.02195	-0.02196
0.5	-0.01157	-0.01158
1.0	-0.02714	-0.02715

4.5. Trapping Phenomena

The streamlines are the imaginary lines in a fluid flow that provide us with the velocity at any location along the streamline. These lines will show the direction of movement of a zero-rest mass fluid element at any point in time. Trapping is the buildup of bolus of fluid in confined streamlines inside a wave frame. The nature of the streamlines against fluid parameter $\Gamma = 0.01, 0.02, 0.03, 0.04$ respectively, is as shown in Figures 6. The fluid's viscosity relies on the parameter Γ , and it comes out to be highly viscous and turns thicker as we enhance the value of the third grade fluid parameter. Moreover, with the raising the values of the fluid parameter, the bolus will drastically shift to the middle of the channel, and the coupling streamlines slight below the wall.

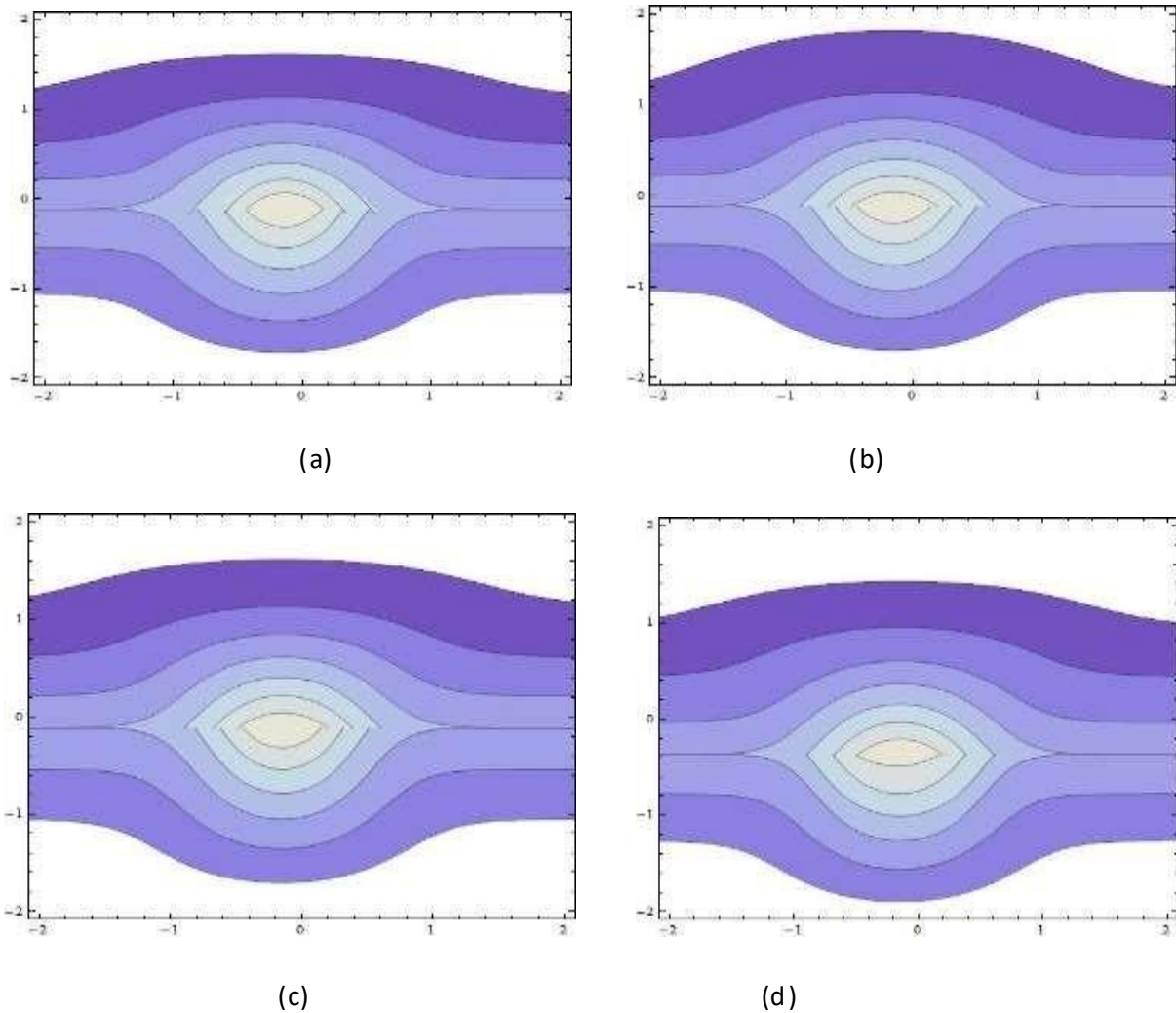


Figure 6. Streamline distribution (ψ) for (a) $\Gamma = 0.01$ (b) $\Gamma = 0.02$ (c) $\Gamma = 0.03$ (d) $\Gamma = 0.04$ while other parameters are $x = 0.2, U = -2, m_e = 2, B_r = 2, M = G_r = S_c = S_r = R_n = P_r = 0.5, G_c = 0.2, \Theta = 2$

5. CONCLUSIONS

In this paper, we explore the magneto-electrohydrodynamic peristaltic transport of a thirdgrade nanofluid flow in the presence of heat radiation in an asymmetric channel. Specifically, we focus on how the flow affects the magneto-electrohydrodynamic peristaltic transport. The effects of various physical parameters on the velocity, temperature, concentration of species, and heat transfer coefficient are explored and graphically examined. The following conclusions are drawn from this work:

- As the magnetic field parameter M increases, the fluid's velocity decreases due to the Lorentz forces, which suppress the fluid motion.
- The magnitude of velocity enhances as the electroosmotic parameter m_e increases. The magnitude of velocity for an asymmetric channel increases by 25% approximately, whereas for a symmetric channel increases by 95%.
- The Deborah number Γ raises the velocity profile in both symmetric and asymmetric channels. The velocity magnitude for an asymmetric channel increases by 20% approximately, whereas for a symmetric channel increases by 63%.
- Both thermal radiation parameter R_n and heat transfer co-efficient Z have decreasing effect on temperature θ .
- Brinkmann number B_r causes the temperature to rise. This behaviour can be explained by greater thermal energy generated due to the viscous dissipation, which reduces the fluid temperature and concentration ϕ .
- Higher values of the Schmidt number S_c and Soret number S_r result in a decrease in concentration. Physically, increasing S_c means decreasing molecular diffusion, which diminishes the concentration.
- The fluid velocity in the channel increases close to the right wall and the left wall as the Grashoff number G_r increases because the buoyant forces take precedence over the viscous forces.
- Deborah number Γ enhances the temperature profile, whereas it diminishes the concentration profile.
- An increase in the values of the fluid parameter Γ , the bolus will drastically shift to the middle of the channel, and the coupling streamlines slight below the wall.

Declaration of Competing Interest

The author declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

Funding Acknowledgement: No

Nomenclature:

ϕ Phase difference

a_1 Amplitude of the upper wall

a_2 Amplitude of the lower wall

\tilde{t}	Time
λ	Wavelength
d_1	Half-width of the upper wall
d_2	Half-width of the lower wall
U	Velocity in X direction
V	Velocity in Y direction
ε	Permittivity of dielectric
ρ_e	Overall density of charges
Φ	Electrical potential
e	Electronic charge
z_v	Charge balance
n_0	Bulk concentration
K_B	Boltzmann constant
T_{av}	Average temperature
m_e	Electro-osmotic parameter
T	Stress tensor
\tilde{I}	Identity tensor
p	Pressure
S	Extra stress tensor
ρ_e	Electric charge density
ρ	Fluid density
E_x	Axial electric field
P	Pressure
σ	Electrical conductivity,
k	Thermal expansion coefficient,
g	Acceleration due to gravity
k'	Concentration expansion co-efficient.
q_r	Radiated heat flux,
k_t	Thermal diffusion,

D_m	Mass diffusivity,
T_m	Average temperature
\tilde{T}	Non-dimensional temperature
\tilde{C}	Non-dimensional concentration
M	Magnetic field parameter
G_r	Grashoff number
G_c	Species concentration Grashoff number
Γ	Deborah number
m_e	Electro-osmotic parameter
S_c	Schmidt number
S_r	Soret number
B_r	Brinkmann number
R_n	Thermal radiation parameter

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